

مادة الرياضيات (السنة الأولى من التعليم المتوسط)

تابع للإنشاءات الهندسية

-
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-
-
-



-
-
-
-
-
-

B A

B A :

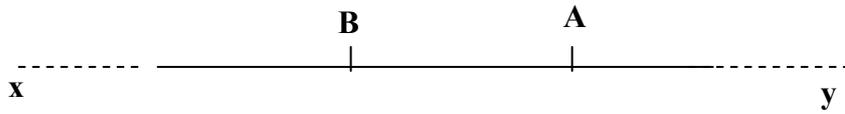
[BA] [AB]

⋮

⋮

:

B A : (xy)



⋮

⋮

:

(xy)

B A



B A

(xy)

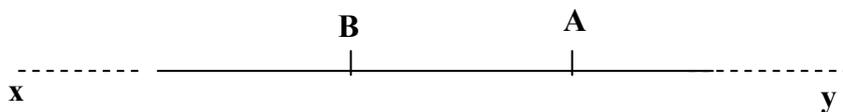
[Ax ∩ [By :

[AB]

[By ∩ [Ax = [AB] :



(xy) A B



[AB]

B A : B A : [AB]



=



[AB] B [AB] A -1

.A ∉ [AB]]AB] :

[AB] [AB[[AB] A [AB] B -2

.B ∉

[AB]]AB[[AB] B [AB] A -3

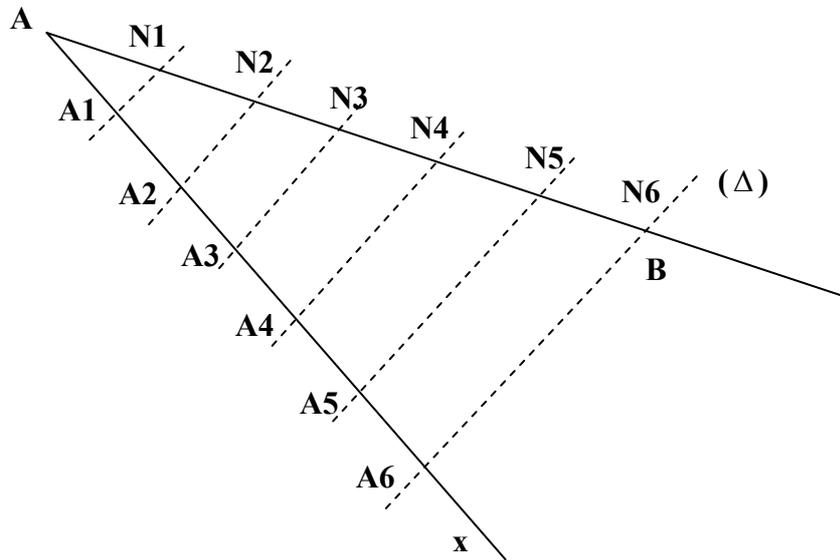
.A ∉ [AB] B ∉

. A ∈ [AB] B ∈ [AB] [AB] : [AB] -4



6

[AB]



[Ax B [Ax -

.H [Ax -

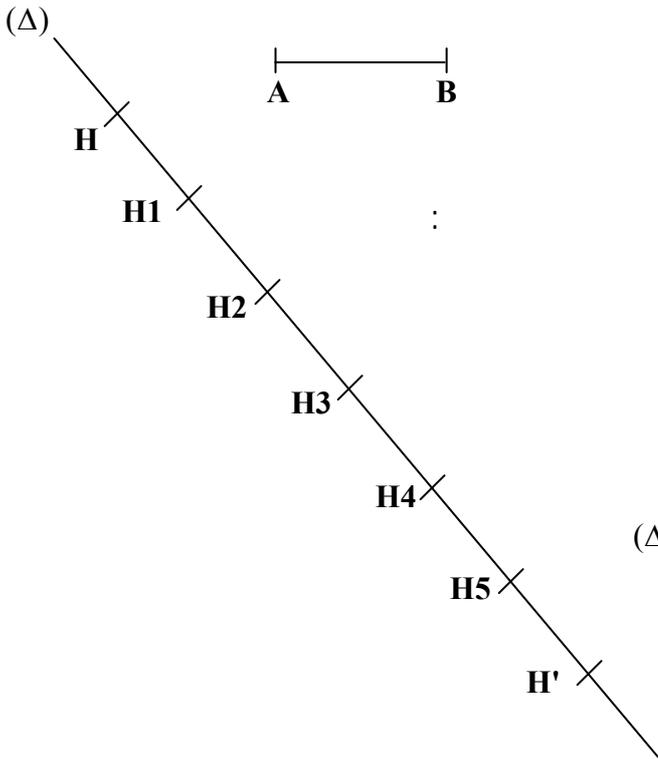
A6 B -

A6 A5 A4 A3 A2 A1 (Δ) -

N6 N5 N4 N3 N2 N1 (AB)

: [AB]

A N1 = N1 N2 = N2 N3 = N3 N4 = N4 N5 = N5 N6



a

[AB]

.a ≠ 1

$$.H H' = a .AB$$

-



(Δ)

H

[AB] ∉ (Δ)

(Δ)

.[AB]

. H1

H

-

H2

H1

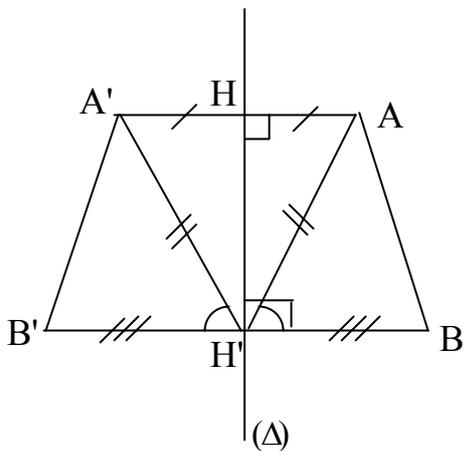
H'... H4 H3

a

.AB

[H'H]

$$.H H' = a .[AB]$$



.[AB]

[A'B']

[AB]

(Δ)

[AB] ∉ (Δ)



.(Δ)

A

A'

.(Δ)

B

B'

B' A'

[A'B']

[AB]

:

$$.AB = A'B'$$

:

:

(

)

$$[BB'] \cap (\Delta) = H' \quad (\Delta) \cap [AA'] = H : \\ AA' H' \quad H' \in (\Delta) \quad [BB'] \quad (\Delta) \quad [AA'] \quad (\Delta)$$

$$(1) \dots \widehat{A'H'H} = \widehat{H'H'A} : \quad \widehat{A'H'A} \quad [H'H] :$$

$$(2) \dots 90^\circ = \widehat{HH'A'} + \widehat{A'H'B'} = \widehat{H'H'A} + \widehat{AH'B} :$$

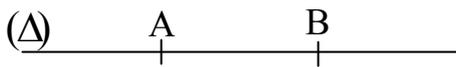
$$\widehat{A'H'B'} = \widehat{AH'B} : \quad (2) \quad (1)$$

. $A'H'B' \quad AH'B$

$$\widehat{A'H'B'} = \widehat{AH'B} \quad \widehat{H'B'} = \widehat{H'B} \quad H'A' = H'A :$$

$$A'B' = AB$$

$$[AB] \subset (\Delta) :$$



. B (Δ) B

A (Δ)

A

$[AB] \subset (\Delta)$

. $[AB]$

.N $\notin [AB] :$

. $[AB]$

$[A'B']$

$[AB]$

N

$[AB]$

:

.N

A

A'

.N

B

B'

. $[A'B']$

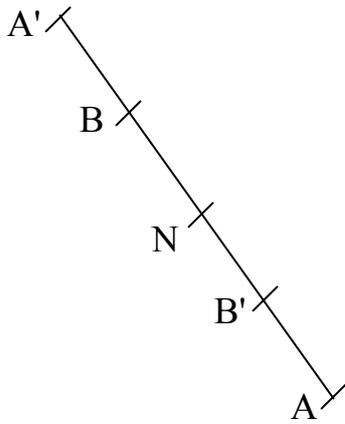
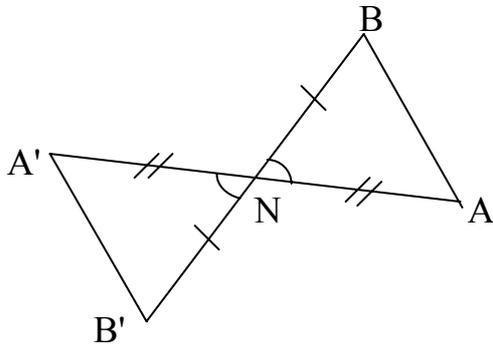
$[AB]$

. $AB = A'B' :$

A' B'

$$\widehat{A'NB'} = \widehat{ANB} \quad NA = NA' \quad NB = NB' : \quad A'NB' \quad ANB$$

$$A'B' = AB$$



.[AB] [A'B']

N ∈ [AB] :

.[AB] N [AB]

.[AB] [A'B']

.N A A'

.N B B'

.[A'B'] [AB] A' B'

:

(1).....(N A A') NA' = NA

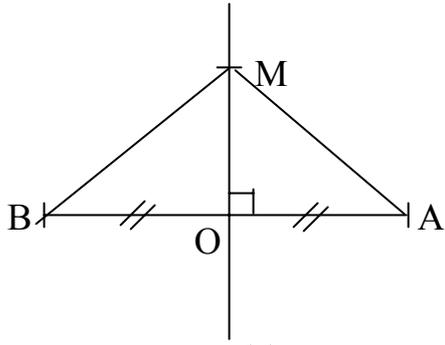
(2).....(N B B') NB' = NB

NA' + NB' = NA + NB : (2) (1)

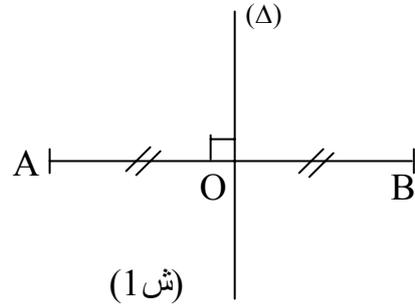
.[A'B'] [AB] AB = A'B'



.[AB] O (AB) (Δ) [AB] (Δ)



(ش 2)



(ش 1)

:1

:

$$M \in (\Delta)$$

$$MA = MB$$

:2

:

.[AB]

M

:1

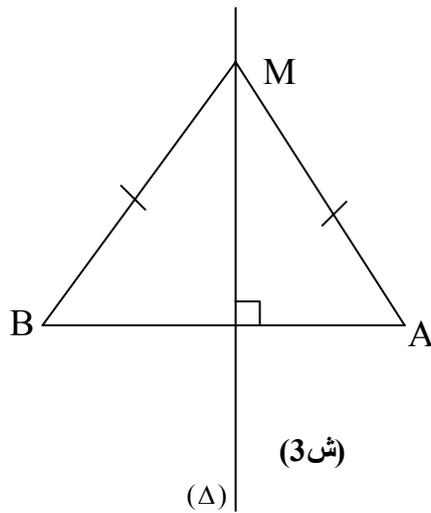
.(Δ)

A B

2 1

(2) .[AB]

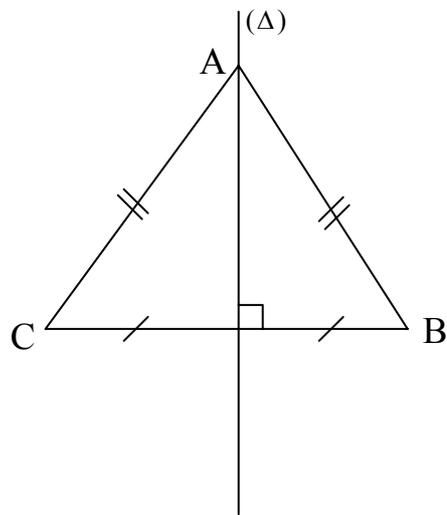
(Δ)



(ش 3)

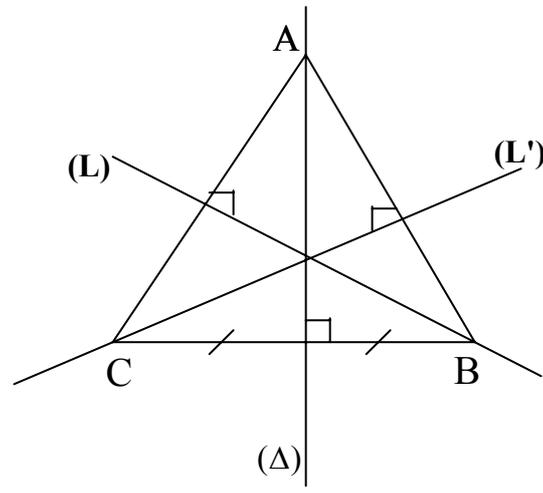
(Δ)

$[AB]$ (Δ) $[AB]$ (Δ) **:2**
 $.[AB]$ (Δ) (Δ) $A B$
 $.(\Delta)$ (Δ)
 $A .(\Delta)$ $C B :$ $[BC]$ (Δ) **-1**
 $.ABC$ $[BC]$ (Δ) $.(\Delta)$

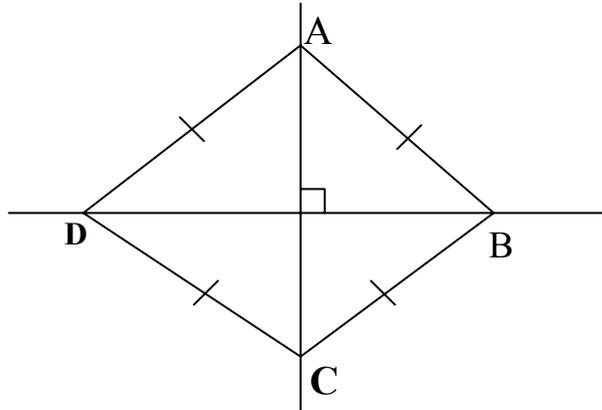


$.$ $:$
 $:$ **-2**

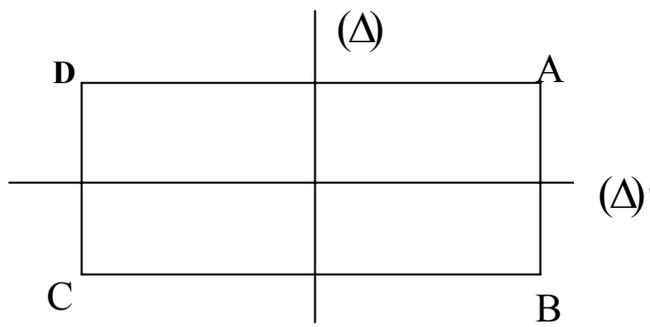
ABC



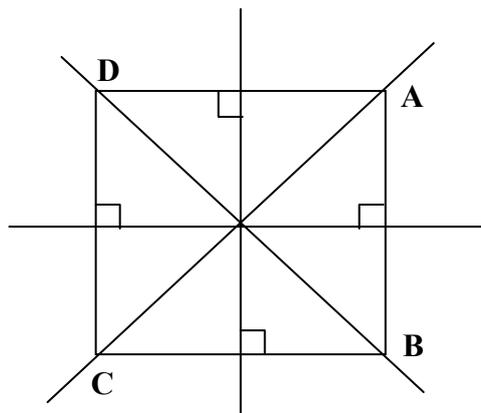
: -3



: -4



: -5



⋮

:

:

-1

:

-2

:

-3

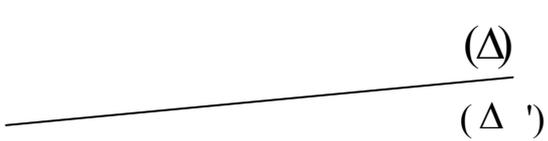
:

⋮

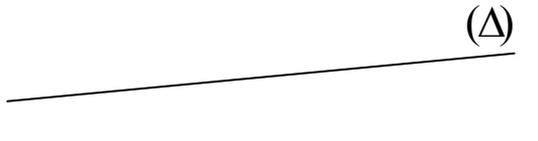
:

(1)

:



(ش 2)



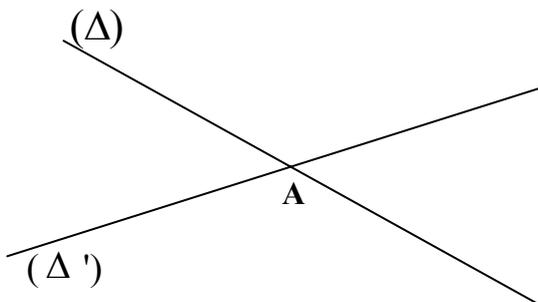
(ش 1)

(Δ') (Δ) :1

(Δ) (Δ') : :2

⋮ (2)

:



ش 3

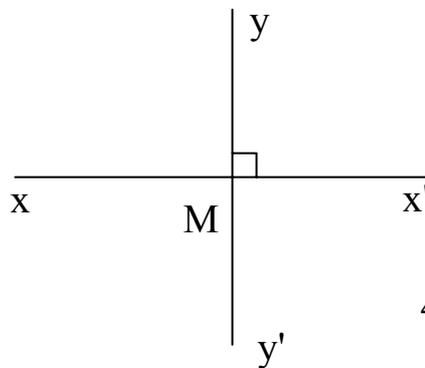
(4) (4)

M

(yy') (xx')

(y y') ⊥ (xx') :

: [redacted]



ش 4

$$[90^\circ = \widehat{xMy} \{M\} = [(xx') \cap (yy')] \Leftrightarrow [(xx') \perp (yy')]$$

:

N (Δ)

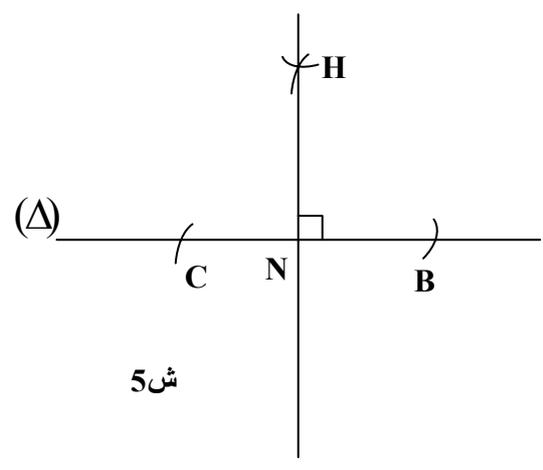
.N ∈ (Δ) :

.C B (Δ) N -

C B -

.H

(Δ) ⊥ (HN) :



.N ∉ (Δ) :

N R C B (Δ) N -

(Δ)

[Nx \widehat{BNC} -

. (Δ) ⊥ [Nx :

(6) (Δ) ⊥ (Nx)

(x y) N (x y) :

.N B (x y) -

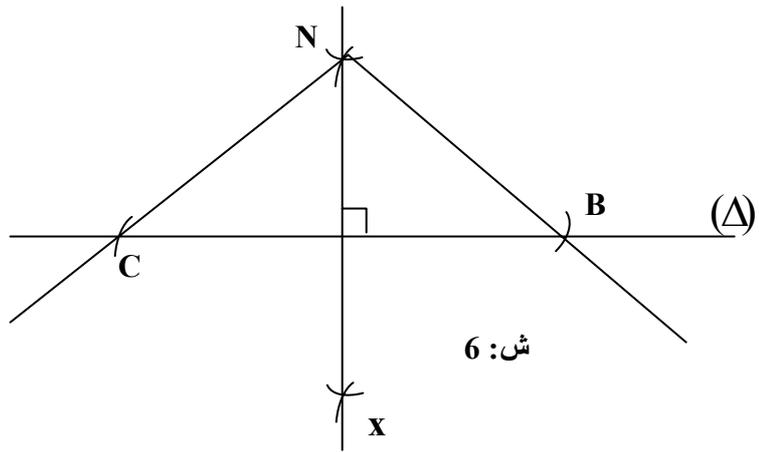
$\widehat{NB y}$ -

.N (x y)

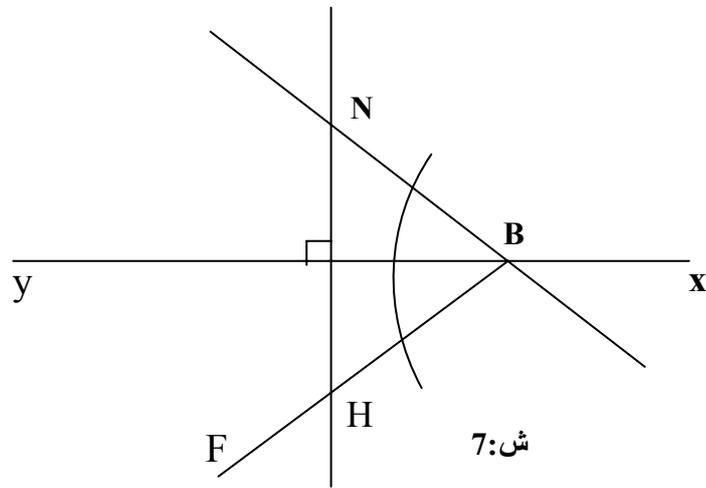
.BN = BH : H -

H ∈ BF

(7) (HN) ⊥ (x y) :



ش: 6



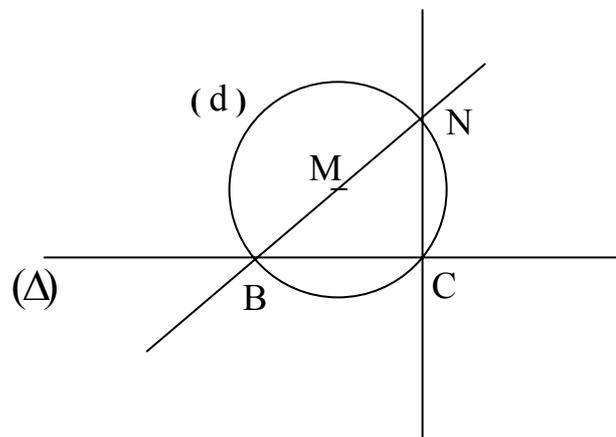
ش: 7

(Δ) N (Δ) :

. N B (Δ) -

. [BN] (d) -

. (Δ) ⊥ (NC) : (d) ∩ (Δ) = {B C} : -



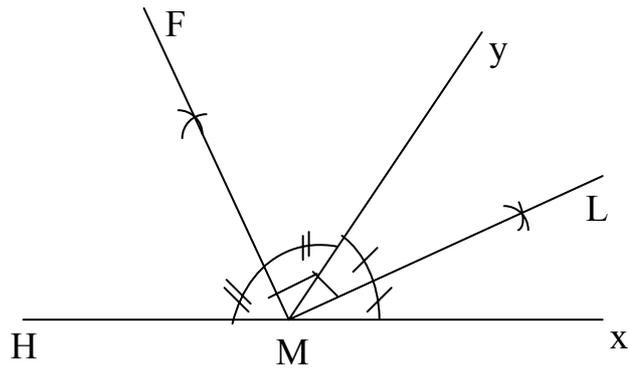


(2)

:

\widehat{yMH} \widehat{xMy}

$(ML) \perp (MF)$ \widehat{yMH} \widehat{xMy} $[MF]$ $[ML]$



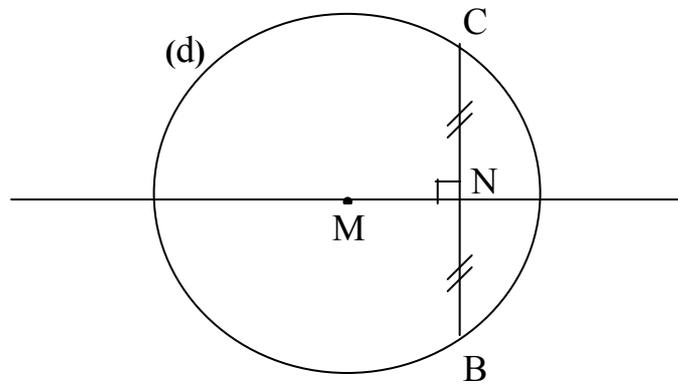
\widehat{M}

:

$d(MR)$

$[BC]$

$(BC) \perp (MN)$: $[BC]$ N



.M' M

C B

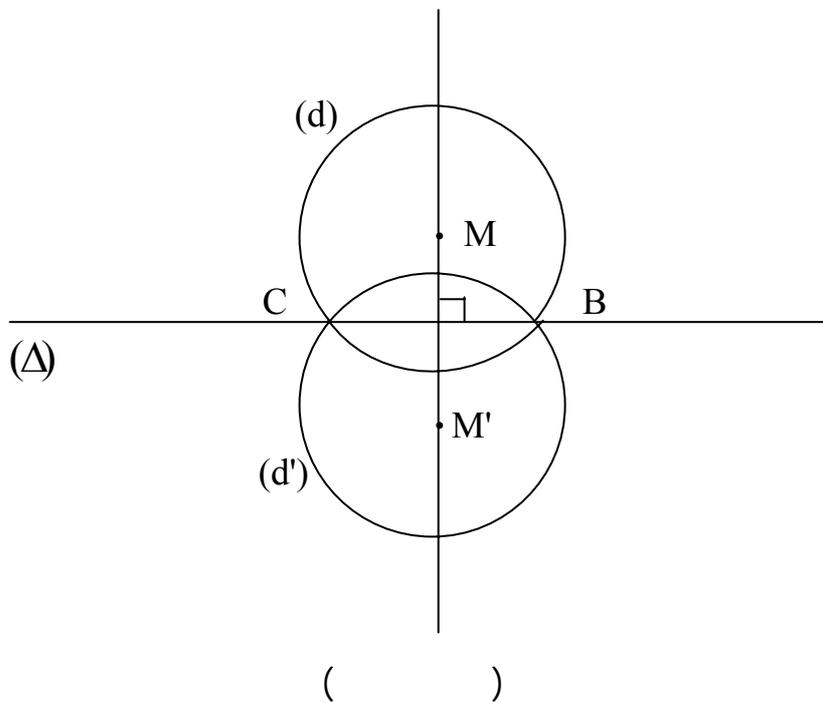
(d') (d)

:

.[BC]

.M' M

(M M') \perp [BC] :



:

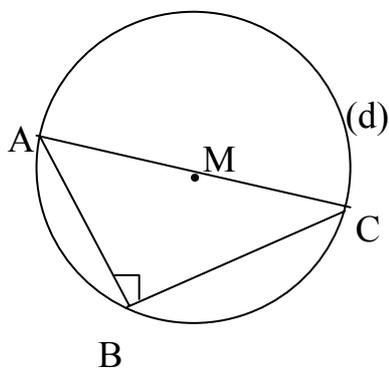
d(M R)

(d) A C

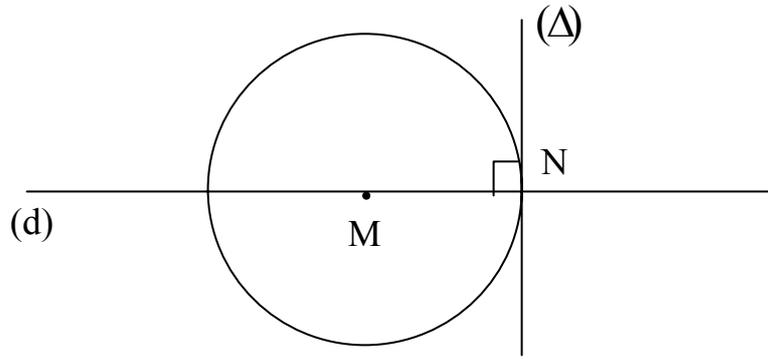
. A C

(d) B

.(BC) \perp (AB) :



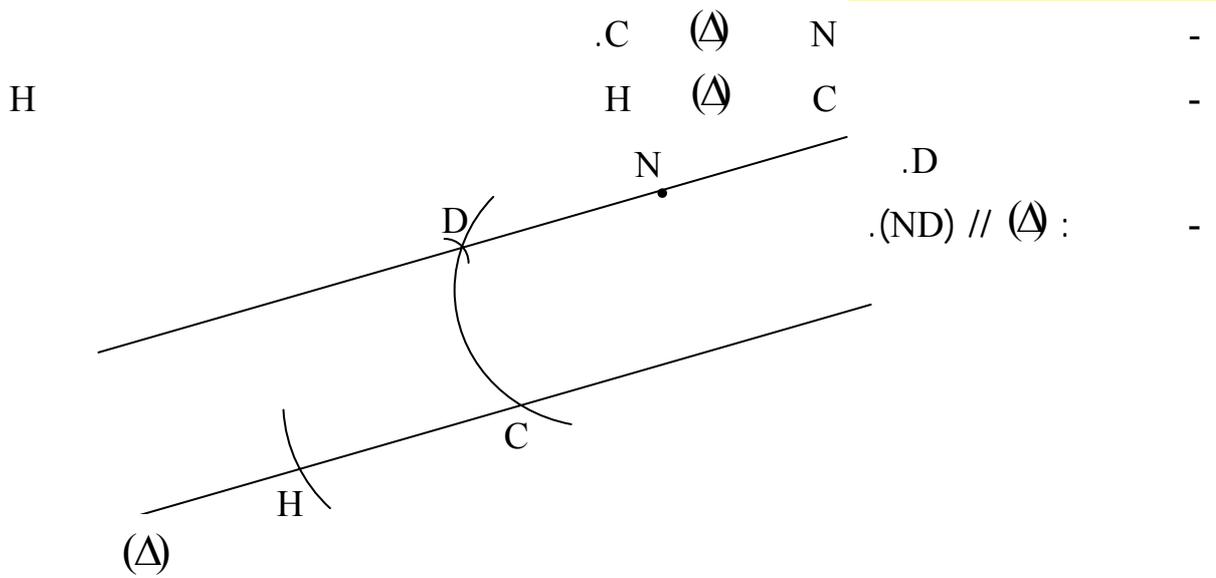
:
 . (M R) -
 (d) N -
 .N (d) (Δ) -
 (Δ) ⊥ (MN) :



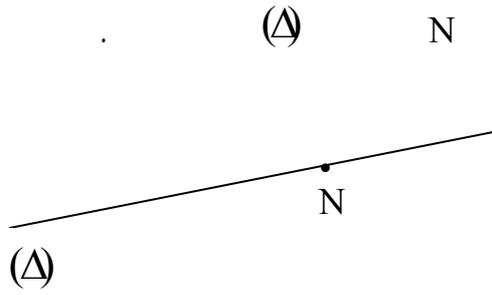
:
 .[(Δ') ⊄ (Δ)] = (Δ') ∩ (Δ) ⇔ [(Δ') // (Δ)]

-1

.N ∉ (Δ) :

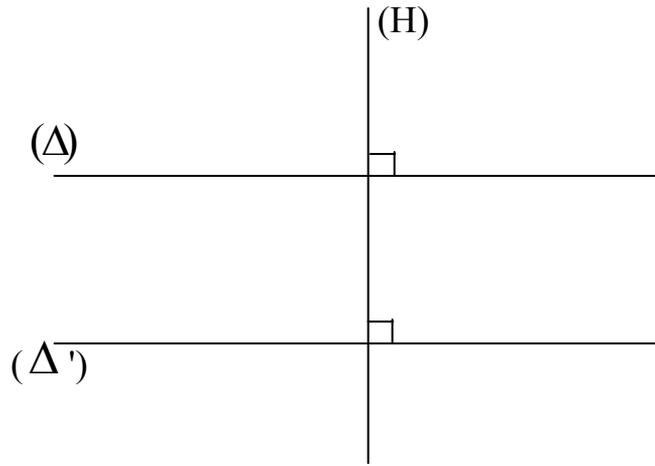


$N \in (\Delta) :$

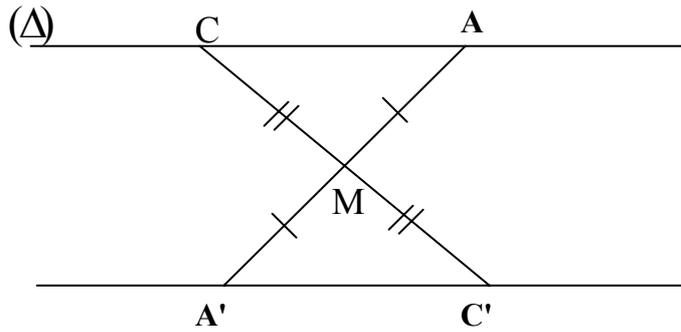


2

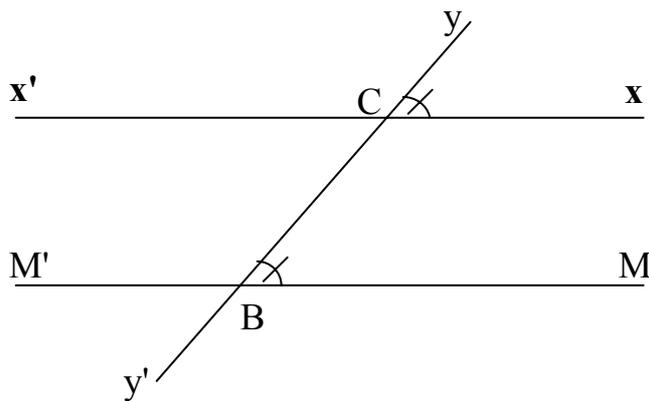
- $(H) \perp (\Delta) \quad (\Delta)$
- $(H) \perp (\Delta) \quad (\Delta) \perp (H) :$
- $(\Delta') \parallel (\Delta) :$



\therefore
 (Δ) -
 $C A$ -
 (Δ) M -
 $C A$ $C' A'$ -
 $(A'C') \parallel (\Delta)$:



\therefore
 (yy') (xx') -
 (yy') B -
 (yy') \widehat{xCy} \widehat{MBy} -
 $(xx') \parallel (BM)$:

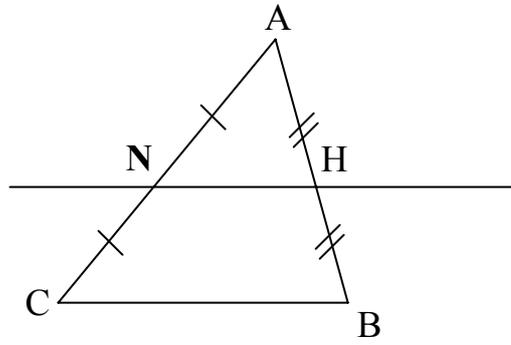


∴

.ABC

[AC] [BA] N H

.(BC) // (HN) :



∴

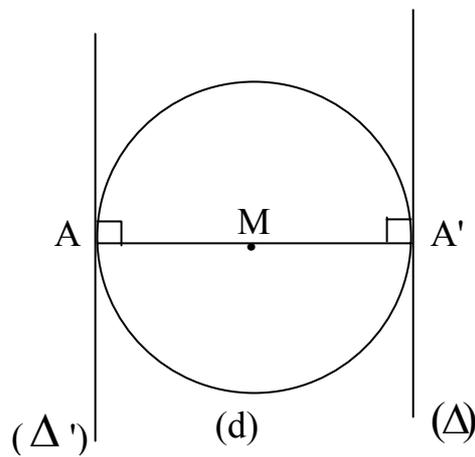
.M (d)

A' A

. A' (d) (Δ)

.A (d) (Δ')

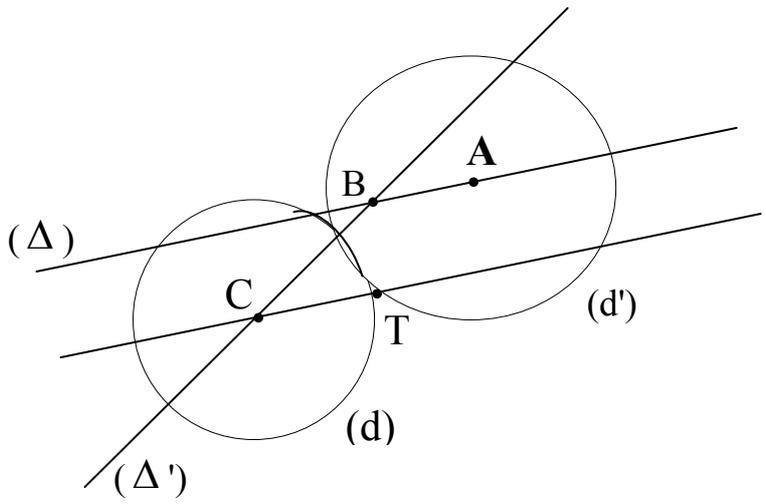
.(Δ') // (Δ) :



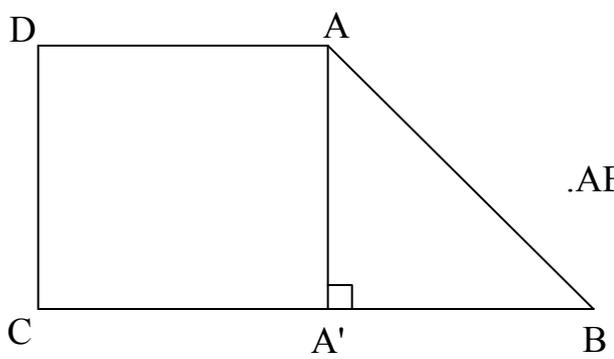
\vdots
 (Δ) B, A
 (B) (Δ) (Δ')
 A,C (d') (d)
 (Δ')
 $[BC], [AB]$

(Δ) T T

.C
 $(\Delta) // (TC) :$



$.ABCD$ $[CB] [DA] :$



$[DC] [DA]$
 AA'



(1)

ABCD

ABC

D

B

ABC

.B

:



.B

ABC

d : (Δ) d

(BC)

A

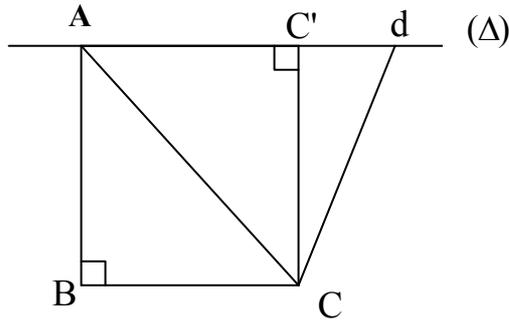
(Δ)

.(Δ)

C

.ABCD

B



(2)

4cm

3cm

. 6cm

:



:

ABC

-

.6cm =

BC=4cm AB=3cm

.B

[AC]

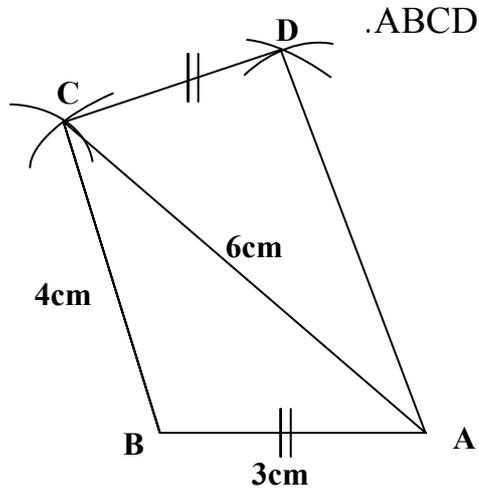
-

.D

C

[AB]

-

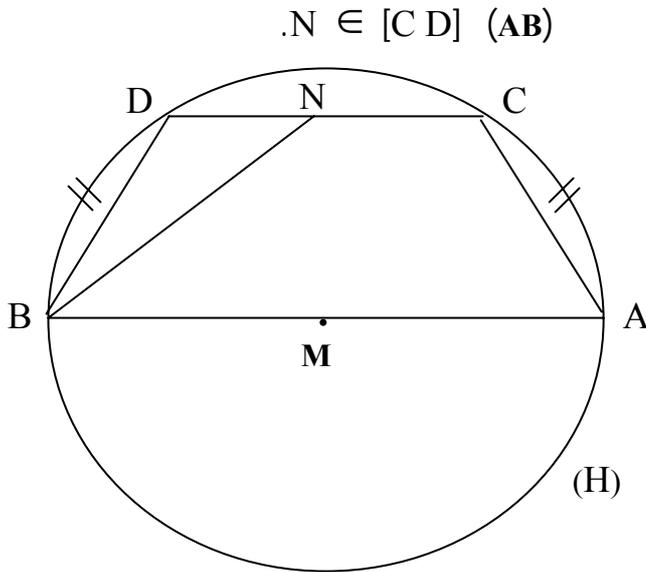


(

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$D \in C$ \widehat{BD} \widehat{AC} : $C \in (H)$ $D \in (H)$ $H(M, \frac{AB}{2})$ (3)

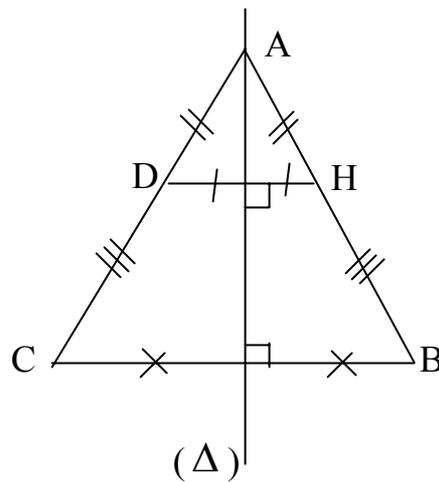


$N \in [CD]$ (AB)

C
 $ABNC$



$[CB]$ ABC
 (Δ)
 $D \in]AB[$ (Δ) H $D, H \in]AB[$
 $HDCB$

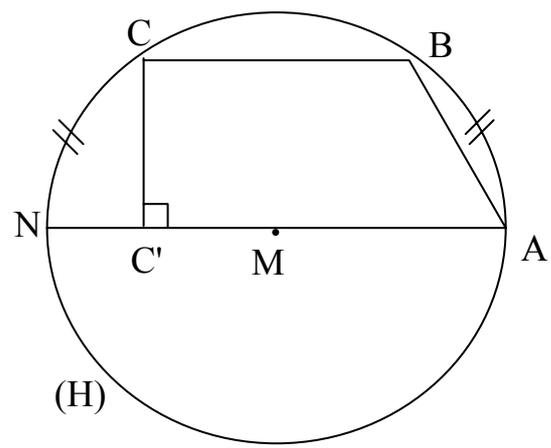




(5)

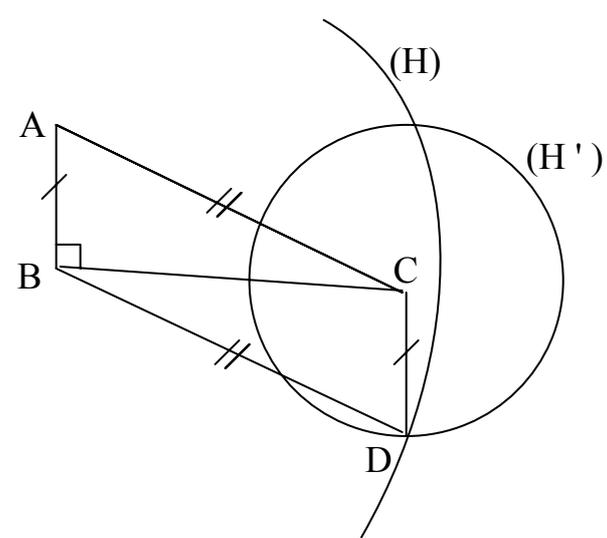
$C \in (H) \quad B \in (H) \quad H \left(\frac{AN}{2}, M \right)$

$C' \in (AN)$
 $ABCC'$
 (AN)

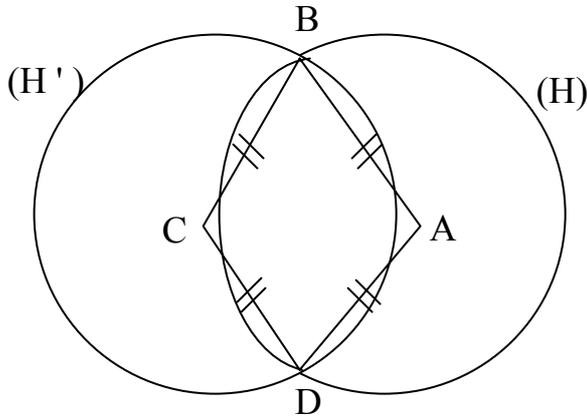


(2)

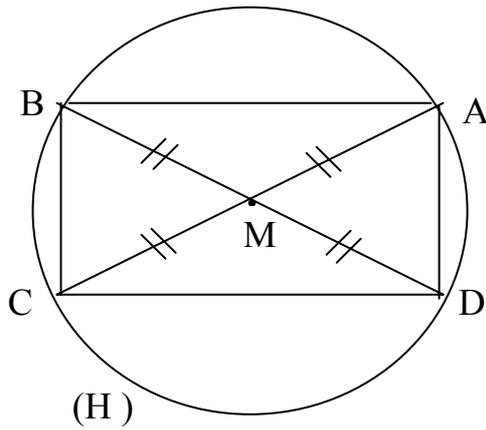
$(H) \cap (H') = \{D\}$
 $H'(C \perp AB) \quad H(B \perp AC)$



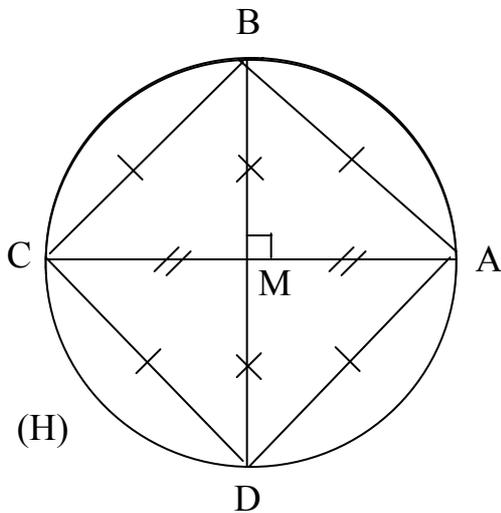
ABDC



$(AC) \perp (BD) : (H)$



$(AC) \perp (BD) : (H)$



(3)
-1

$H'(C R) H(A R)$ A C
 $(H) \cap (H') = \{B D\}$
 ABCD

-2

$[BD] [AC] H(M R)$
 ABCD

-3

$[BD] [AC] H(M R)$
 ABCD